

# Optimal Allocation of DSTATCOM in Distribution Network Using Whale Optimization Algorithm

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**Abstract**—This paper deals with a new approach implemented to decrease power losses and improve voltage profile in distribution networks using Distribution STATic COMPensator (DSTATCOM). DSTATCOM location can be determined by the voltage stability index (VSI) and sizing can be identified by nature inspired, recently developed whale optimization algorithm (WOA). To check efficacy, the proposed technique is tested on two standard buses: Indian rural electrification 28-bus and IEEE 69-bus distribution systems. Obtained results show that optimal allocation of DSTATCOM effectively reduces power losses and improves voltage profile.

**Keywords**—whale optimization algorithm (WOA); voltage stability index (VSI); Distribution STATic COMPensator (DSTATCOM); radial distribution system (RDS)

## I. INTRODUCTION

High R/X ratio in distribution networks causes poor power quality in a distribution system [1]. Its major drawbacks are voltage drop, lagging power factor and instability. These issues create large power losses, poor voltage profile and create network security problems in rural distribution network (RDS). In total power generation 10–13% is consumed as losses in distribution [2–6]. Aforesaid problems can be resolved by adequate reactive power injection in the distribution system. The reactive power can be injected in the RDS with the help of compensating devices. So, compensating devices are essential in the distribution system to decrease power losses and increase the voltages between buses [7]. The majorly of compensating devices used in the RDS are shunt capacitors, regulators, UPFC, SSSC, and DSTATCOM [8]. DSTATCOMs have many advantages over other compensating devices, like low power losses, less harmonic production, compact size and low cost. In addition, they will not create any operation problems like resonance or harmonics [9]. A DSTATCOM consists of a shunt connected voltage source converter (VSC) which is capable, by compensating the bus voltage, to provide enhanced power factor and reactive power compensation in the RDS. A new strategy can be designed for determining the location and size of DSTATCOM to reduce system power loss, improve voltage profile, power factor, load balancing and power quality, free

from distribution line overloading, enhance system stability, decrease pollutant emissions, and increase system efficiency [10].

Several optimization techniques and compensating devices have been introduced to reduce power loss in the distribution side via optimal DSTATCOM placement: Immune algorithm (IA), differential evolution algorithm (DEA), particle swarm optimization (PSO), genetic algorithm (GA), bat algorithm (BA), harmony search algorithm (HSA) [7–13]. Whale optimization algorithm (WOA) has not yet been utilized for finding the location of DSTATCOM in the RDS. In this work DSTATCOM is introduced for reducing total power loss in RDS by using the WOA. This proposed optimization algorithm is developed on the activities and performance behavior of the whales. WOA is effectively utilized for finding the optimal size and location of the DSTATCOM in a distribution network. This biological based algorithm effectively reduces the exploration area. This method is tested on standard 28-bus and 69-bus test systems by considering minimization loss and voltage stability enhancement. Obtained results by WOA are compared with the results taken from IA and GA. When compared to these existing algorithms, WOA effectively reduces losses and increases voltage stability.

## II. PROBLEM FORMULATION

Newton–Raphson, Gauss-Seidal and fast decoupled are a few classical load flow methods, which are not suitable in identifying the line flows and voltages in distribution networks because of the high resistance by reactance ratio (R/X) of the distribution system. So, the forward-backward sweep distribution load flow is used in the present work to solve the load flow [15]. At node  $t$ , the equivalent injected current is specified as:

$$I_t = \left( \frac{P_t + jQ_t}{V_t} \right) \quad (1)$$

By applying Kirchhoff's current law amongst the buses  $t$  and  $t+1$  in line section, the branch current is set as:

$$I_{t,t+1} = I_{t+1} + I_{t+2} \quad (2)$$

By the usage of bus injected in the direction of branch current matrix (BIBC), (2) is resulted into matrix format:

$$|J| = |BIBC||I| \tag{3}$$

For calculation of voltage at buses  $t+1$ , Kirchoff's voltage law is employed and the equation is specified as:

$$V_{t+1} = V_t - J_{t,t+1}(R_{t,t+1} + jX_{t,t+1}) \tag{4}$$

In the middle of line section buses  $t$  and  $t+1$ , the real reactive power loss will be computed as:

$$P_{Loss(t,t+1)} = \left( \frac{P_{t,t+1}^2 + Q_{t,t+1}^2}{|V_{t,t+1}|^2} \right) * R_{t,t+1} \tag{5}$$

$$Q_{Loss(t,t+1)} = \left( \frac{P_{t,t+1}^2 + Q_{t,t+1}^2}{|V_{t,t+1}|^2} \right) * X_{t,t+1} \tag{6}$$

Total power loss  $P_{TLoss}$  in the system is calculated by summing up of all losses in every line section:

$$P_{TLoss} = \sum_{t=1}^{nb} P_{(Loss,t,t+1)} \tag{7}$$

A. Objective Function

Objective function's mathematical formulation is stated as:

$$Min(F) = \min\left(\frac{P_{Loss}}{VSI}\right) \tag{8}$$

where  $P_{T,loss}$  is the total power loss of the radial distribution system.

B. Constraints

Additional inequality constraints are also considered for this problem. These are:

1) Voltage Deviation Limit:

$$V_t^{min} \leq |V_t| \leq V_t^{max} \tag{9}$$

where  $V_t^{min}$  and  $V_t^{max}$  are the minimum and maximum voltage limits at bus  $t$ , respectively.

2) Reactive Power Compensation:

$$Q_{DSTATCOM(t)}^{min} \leq Q_{DSTATCOM(t)} \leq Q_{DSTATCOM(t)}^{max} \tag{10}$$

$t = 1, 2, \dots, nb$

where  $Q_{DSTATCOM(t)}^{min}$  and  $Q_{DSTATCOM(t)}^{max}$  are the minimum and maximum reactive power limits at bus  $t$ , respectively.

C. Voltage Stability Index

In order to discover the node, VSI is used. At each node, voltage stability is calculated with the aid of (11). The less significance VSI node will be the appropriate locality for the employment of DSTATCOM [16]. To avoid the probabilities of voltage collapse, VSI will be maximized.

$$VSI(m+1) = |V_m|^2 - 4 \left[ \frac{P_{m+1,eff} * X_m - Q_{m+1,eff} * R_m}{P_{m+1,eff} + R_m * Q_{m+1} + X_m} \right]^2 \tag{11}$$

III. WHALE OPTIMIZATION ALGORITHM

WOA is a biological based optimization algorithm which is developed on humpback X behavior of whales. Certain brain cells of whales and human beings are similar. The special

behavior of whales in search for food is called bubble-net feeding method. The searching method is based on creating bubbles by encircling or through a '9'-shaped path. This behavior of searching is derived mathematically by two phases [17]:

A. Searching and Encircling Prey

Searching prey can be modeled by (12) and (13), where variables  $A$  and  $C$  are coefficient vectors denoted as in (14) and (15):

$$D = |C * X_{rand} - X| \tag{12}$$

$$X(t+1) = X_{rand} - A * D \tag{13}$$

$$A = 2 * a * r - a \tag{14}$$

$$C = 2 * r \tag{15}$$

where  $a$  is linearly decreasing from 2 to 0 and  $r$  is a random number between [0, 1].

$$D = |C * X^*(t) - X(t)| \tag{16}$$

$$X(t+1) = X^*(t) - A * D \tag{17}$$

If  $A \geq 1$ , searching prey, denoted by (12) and (23), otherwise encircling prey, by shrinking mechanism denoted by (16) and (17), are used, where  $t$  is the current iteration,  $X$  is the position vector and  $X^*$  is the best value of the position vector so far.

B. Spirally Updating Position

Position updating is denoted by (18):

$$X(t+1) = \begin{cases} X^*(t) - A * D, & \text{if } p > 0.5 \\ D * e^{bl} * \cos(2\pi l) + X^*(t), & \text{if } p \leq 0.5 \end{cases} \tag{18}$$

where  $p$  is a random number between [0, 1],  $l$  is between [-1, 1] and  $b$  is constant for describing the spiral shape [18].

C. Proposed Work Implementation

WOA approach to reduce power losses and enhance voltage profile by placing DSTATCOM optimally in the network is described by the following steps:

- Step 1: Set load data and bus data.
- Step 2: Estimate the total power loss, VSI and bus voltages using forward-backward sweep method.
- Step 3: Read line and load data of the system and solve the feeder-line flow for the system using load flow method.
- Step 4: Find the best DSTATCOM locations using VSI.
- Step 5: Set the population/solutions itmax=100, number of DSTATCOM locations d=1, DSTATCOM Min=20, DSTATCOM Max=2000
- Step 6: Generate the population of DSTATCOM sizes randomly using :

$$\text{Population} = (\text{DST}_{\max} - \text{DST}_{\min}) \times \text{rand}() + \text{DST}_{\min}$$

where  $\text{DST}_{\max}$  and  $\text{DST}_{\min}$  are minimum and maximum limits of DSTATCOM sizes.

- Step 7: Find power losses for generated population.
- Step 8: Current best solution is DSTATCOM values with low losses.
- Step 9: Whales position can be updated through (13) – (15)
- Step 10: From updated population, losses can be determined, by load flow method.
- Step 11: If acquired losses are less, then substitute with current best solution or else repeat step 9.
- Step 12: Display the results if maximum iterations number is reached.

#### IV. RESULTS AND DISCUSSION

In this paper, WOA is implemented for 28-bus and 69-bus systems. In these test systems, three different cases are analyzed to show the effectiveness of the proposed method as shown in Tables I and II, namely a system without DSTATCOM, system with single DSTATCOM, and system with multiple DSTATCOMs. To show the advantage of WOA, the simulation results of WOA are matched with the ones from other existing optimization methods. The results produced by WOA are better than the ones acquired with other optimization methods.

##### A. 28-Bus Indian Rural Distribution Network

To evaluate the capability of the proposed method in real time systems, an 11kV, 28-bus rural Indian distribution system has been taken and tested. The network is radial in nature with 28 buses and the substation linked at first bus as displayed in Figure 1. Essential load and bus data of power lines are taken from [19].

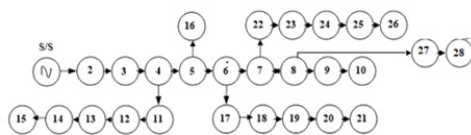


Fig. 1. One line diagram of 28-bus Indian distribution network

##### 1) Case (i) System without DSTATCOM

The initial power losses without using any DSTATCOM in the radial network are 68.88kW. Performance analysis of the 28-bus test system in terms of power losses and voltage stability index with and without DSTATCOM are displayed in Table I.

##### 2) Case (ii) System with Single DSTATCOM.

By this process, the 7<sup>th</sup> bus is designated as an optimal DSTATCOM installation and the optimal place of this location can be designed through WOA. The power losses are reduced to 36.89kW from 68.88kW and the voltage profile is greatly improved. The least bus voltage is obtained by placing single DSTATCOM is 0.9472p.u.

##### 3) Case (iii) System with Multiple DSTATCOMs

By this process, two DSTATCOMs are optimally placed and sized at 7<sup>th</sup> and 12<sup>th</sup> bus. From Table I, it is observed that power loss reduction and voltage stability enhancement are high in multiple DSTATCOM placement compared with single DSTATCOM placement. Power losses are reduced to 33.75kW and the VSI is improved to 0.8035p.u with multiple DSTATCOM placement. Also the minimum bus voltage enhanced from 0.9123p.u to 0.9495p.u. Figure 2 shows the voltage profile improvement of 28-bus with and without single and multiple DSTATCOM placement. The voltage profile is greatly improved with the placement of multiple DSTATCOM's compared to single DSTATCOM placement. We did not compare the proposed method with existing ones, since there is no work available with DSTATCOM placement for 28-bus system in the related literature.

TABLE I. 28-BUS TEST SYSTEM PERFORMANCE ANALYSIS

Proposed Method		
<b>Case (i): Without Compensation</b>	$P_{\text{loss}}$ (kW)	68.88
	CVD	1.7975
	$VSI_{\min}$ (p.u)	0.6927
	$V_{\min}$ (p.u)	0.9123
<b>Case (ii): With single DSTATCOM</b>	Size in kVAr (location)	580 (7)
	$P_{\text{loss}}$ (kW)	36.89
	% $P_{\text{loss}}$ Reduction	46.44
	Total CVD	0.3093
	$VSI_{\min}$ (p.u)	0.7999
	$V_{\min}$ (p.u)	0.9472
<b>Case (iii): With Multiple DSTATCOMs</b>	Size in kW (location)	480 (7), 230 (12)
	$P_{\text{loss}}$ (kW)	33.75
	% $P_{\text{loss}}$ Reduction	51
	TVD	0.2076
	$VSI_{\min}$ (p.u)	0.8035
	$V_{\min}$ (p.u)	0.9495

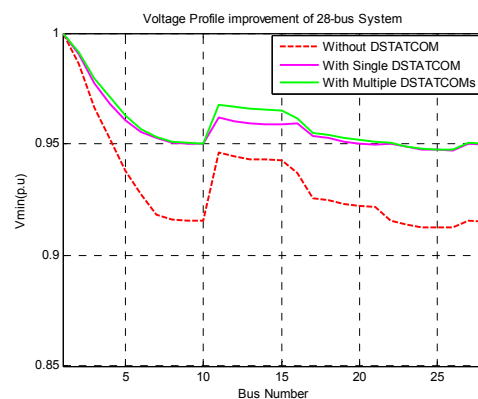


Fig. 2. Voltage profile improvement of 28-bus

##### B. IEEE 69-Bus Distribution Network

To evaluate WOA in a high level system, an 11 kV, IEEE 69-bus has been taken and tested. The required load and bus

data of power lines are taken from [9]. The real and reactive load are 3801kW and 2694.6kVAr and the base values are 100MVA, 12.66KV. The real and reactive power losses of the base case are 225kW and 102.2kVAr. The one line diagram of IEEE 69-bus is depicted in Figure 3. Performance analysis of the IEEE 69-bus test system with and without compensation in terms of power losses, kVAr, VSI, and voltage profile is shown in Table II.

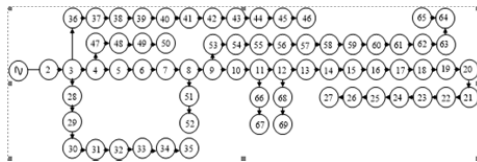


Fig. 3. One line diagram of IEEE 69-bus

TABLE II. 69-BUS TEST SYSTEM PERFORMANCE ANALYSIS

		Proposed Method	IA [9]	GA [9]
<b>Case (i): Without Compensation</b>	$P_{loss}$ (kW)	225	225	225
	Total CVD	0.7327	0.7327	0.7327
	$VSI_{min}$ (p.u)	0.6822	0.6822	0.6822
	$V_{min}$ (p.u)	0.9090	0.9090	0.9090
<b>Case (ii): With single DSTATCOM</b>	Size in kVAr (location)	1300 (61)	1704 (61)	1928 (61)
	$P_{loss}$ (kW)	151.09	157.50	165.43
	% $P_{loss}$ Reduction	32.84	30	26.47
	Total CVD	0.5162	-----	-----
	$VSI_{min}$ (p.u)	0.7584	0.7561	0.7534
$V_{min}$ (p.u)	0.9389	0.9353	0.9380	
<b>Case (iii): With Multiple DSTATCOMs</b>	Size in kW (location)	350 (17), 1250 (61)	---	---
	$P_{loss}$ (kW)	146.34	---	---
	% $P_{loss}$ Reduction	34.96	---	---
	Total CVD	0.5011	---	---
	$VSI_{min}$ (p.u)	0.7630	---	---
$V_{min}$ (p.u)	0.9417	---	---	

1) Case (i) System without DSTATCOM

The initial power loss without any compensation is 225kW.

2) Case (ii) System with single DSTATCOM.

In this process, the 61<sup>st</sup> bus is designated for optimal DSTATCOM installation using VSI and the optimal placing of this location can be designed through WOA. The real power loss in this case is reduced to 151.09kW. The minimum bus voltage obtained from this case is 0.9299p.u.

3) Case (iii) System with Multiple DSTATCOMs

In this test case, DSTATCOMs are optimally placed and sized at 17<sup>th</sup>, and 61<sup>th</sup> buses. From Table II, it is observed that power loss reduction and voltage stability enhancement are high in multiple DSTATCOM placement compared with single DSTATCOM placement. The power loss is reduced to

34.96kW which is high compared with case (ii). The stability value of the system is improved from 0.6822p.u to 0.7630p.u. To show its effectiveness, the proposed WOA is compared with IA and GA [9]. It could be concluded that the proposed WOA gives better loss reduction, stability improvement and voltage enhancement compared with existing algorithms.

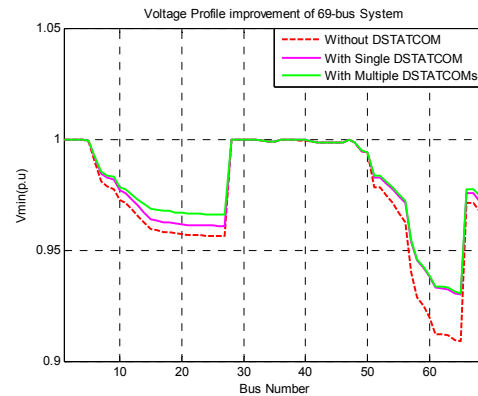


Fig. 4. Voltage profile improvement of 69-bus system

V. CONCLUSION

Whale optimization algorithm has been implemented and tested in Indian 28-bus and IEEE 69-bus radial distribution systems. To find the optimal location of the DSTATCOM, VSI method was used. To find optimal size of DSTATCOM, WOA was used. The power loss was reduced and voltage profile was improved. The proposed method resulted in better power loss reduction and improved the voltage profile than other existing techniques. Hence, the proposed method can be implemented for any distribution system to reduce power loss and enhance voltage profile.

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